



# How validation through model exploration empowers theories of spatial complexity: example of urban systems

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*DAFNI, 22/11/2021 ISC-PIF-UCL*

# How to explain urban growth?

- Apparent direct **causes** : intentions/actions from urban actors (policies, locational strategies from firms, residential migrations...)
- But **statistical observation** (thousands of cities, over centuries) : each city has a probability of growing similar to other cities belonging to the same territorial system
  - = « **distributed growth** » on the long run with many local and temporal **fluctuations**

# Statistical formalization

## Gibrat's model

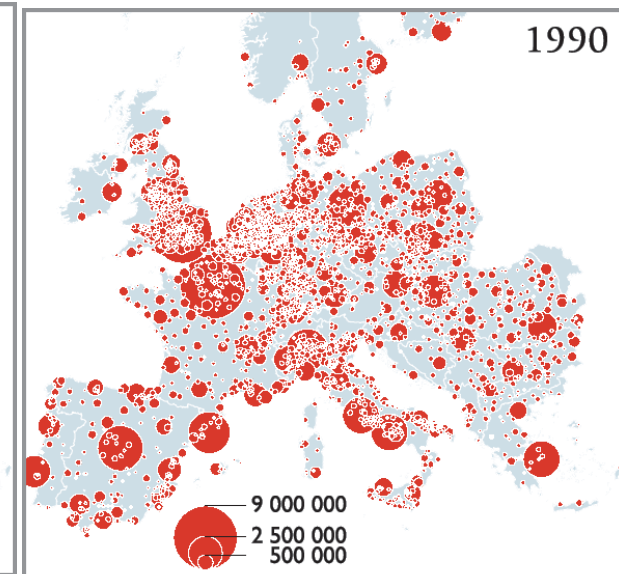
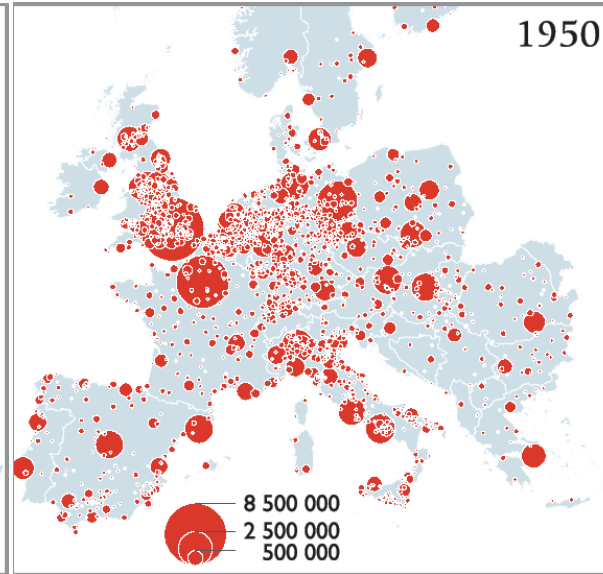
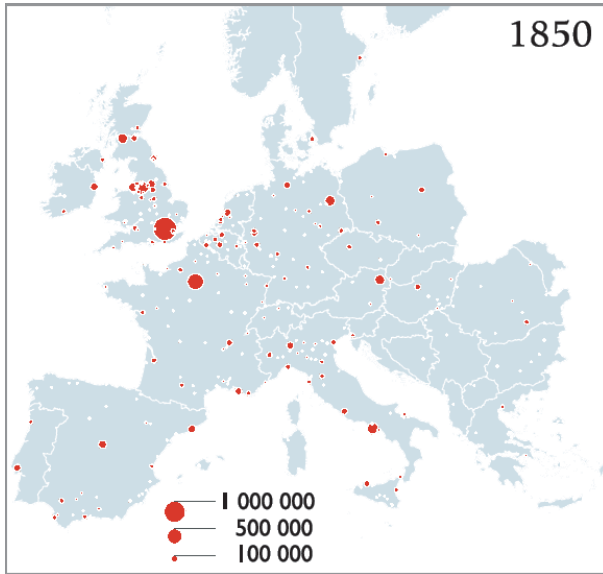
(« proportional » growth = growth rates are equiprobable  
∀ city size and not correlated with previous rate)

Good fit → double gain in explaining:

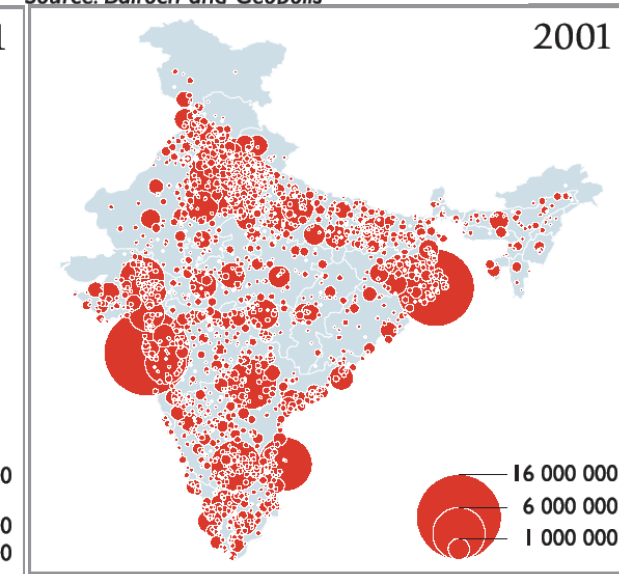
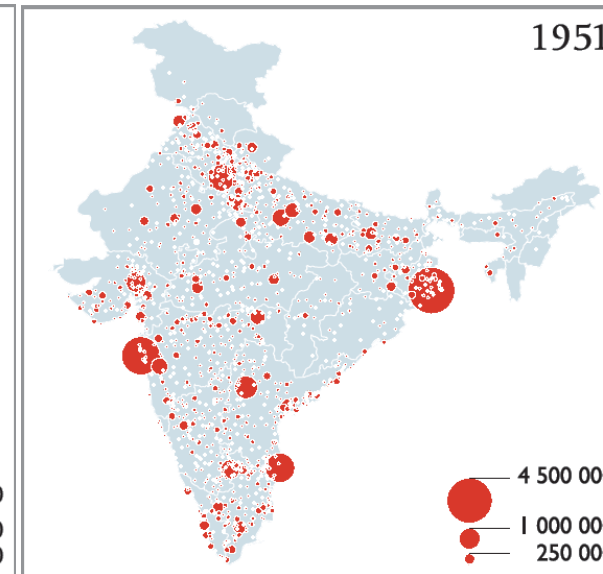
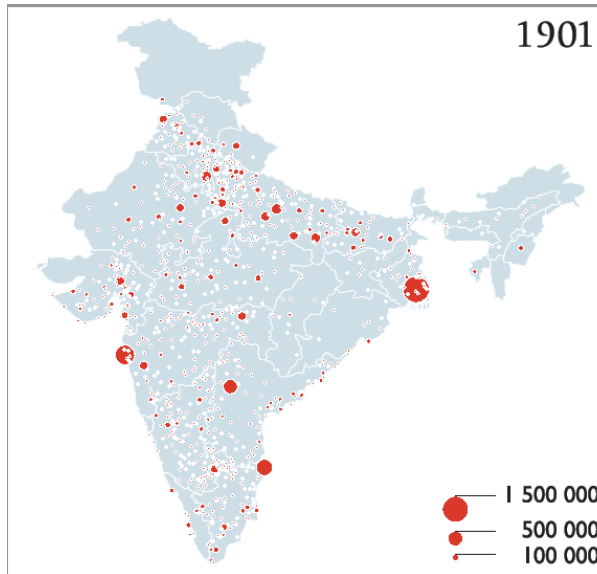
- Persistency of urban spatial patterns and hierarchies
- The statistical shape of urban sizes distribution (Zipf's law or lognormal  $\approx$  H. Simon  $\neq$  P. Krugman) as generated from growth process

[Gibrat, 1931, Robson, 1973, Pumain, 1982]

# Persistency: Europe and India



Source: Bairoch and Geobolis 500 km



Source: Census of India 250 km

[Bretagnolle et al., Cybergeog, 2002]

# Persistency: former Soviet Union

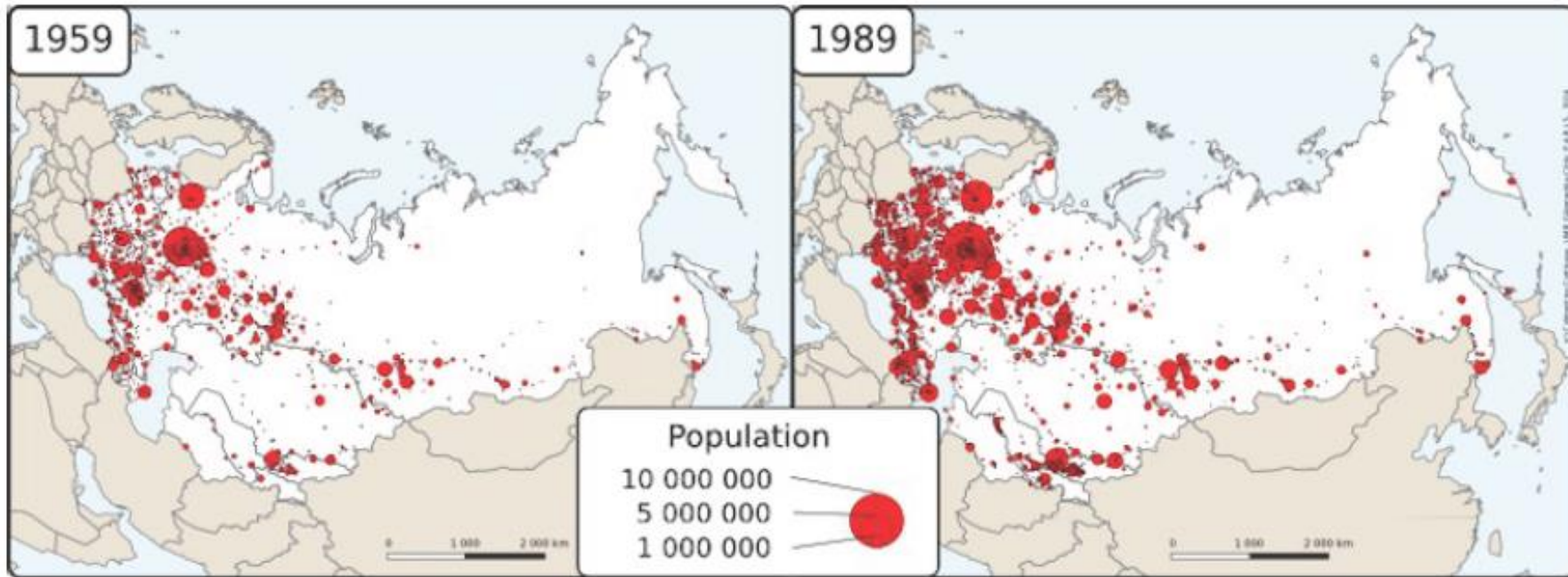
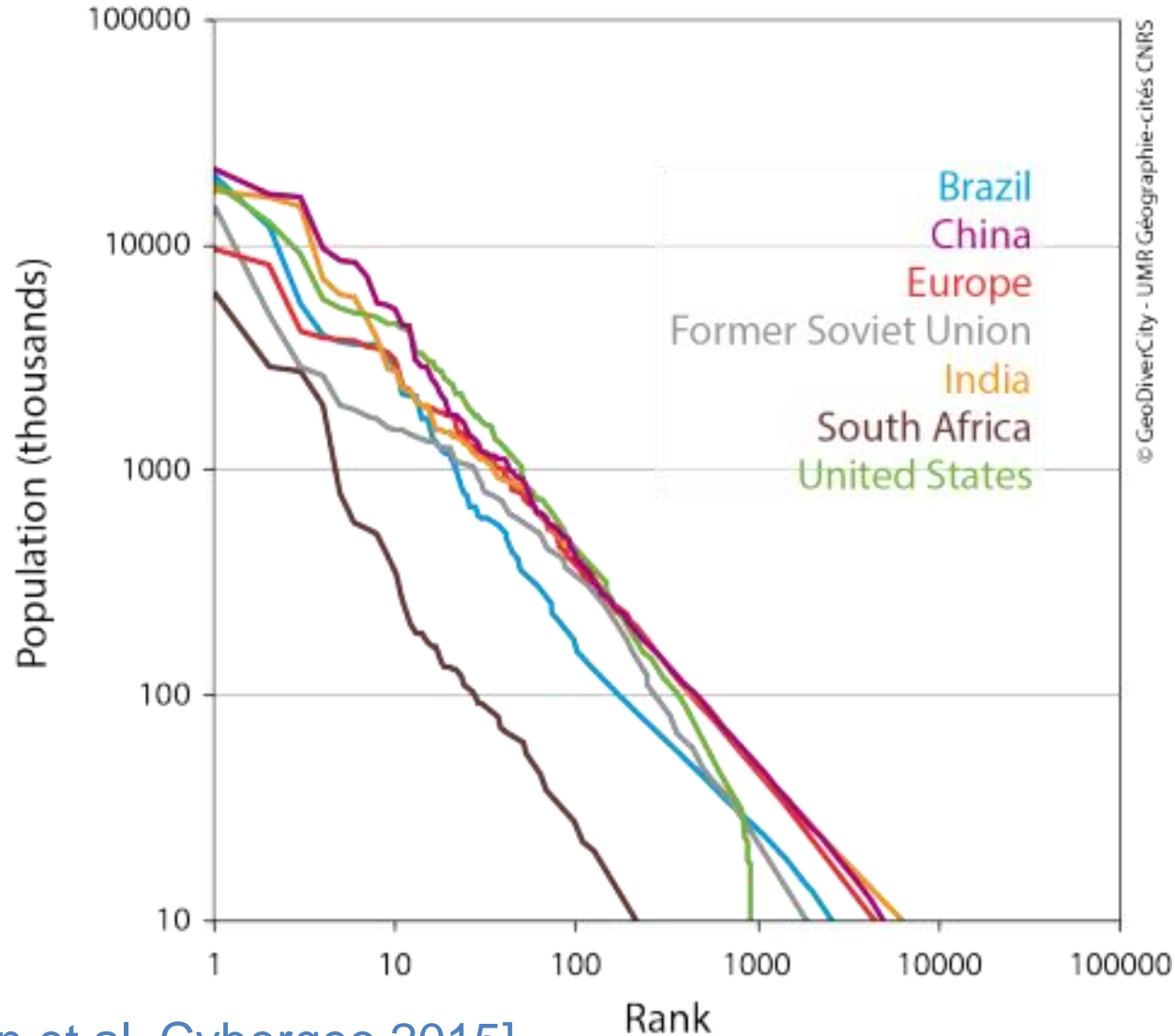


Figure 2. Empirical spatial and hierarchical distribution of cities in the post-Soviet space  
source: DARIUS, 2014

[Cottineau et al., 2015, JASS]

# Zipf's law for 7 systems of cities

Zipf's law:  
Urban sizes  
continuum  
over more than  
4 orders of magnitude  
( $10^3$  à  $10^7$  inhab.)

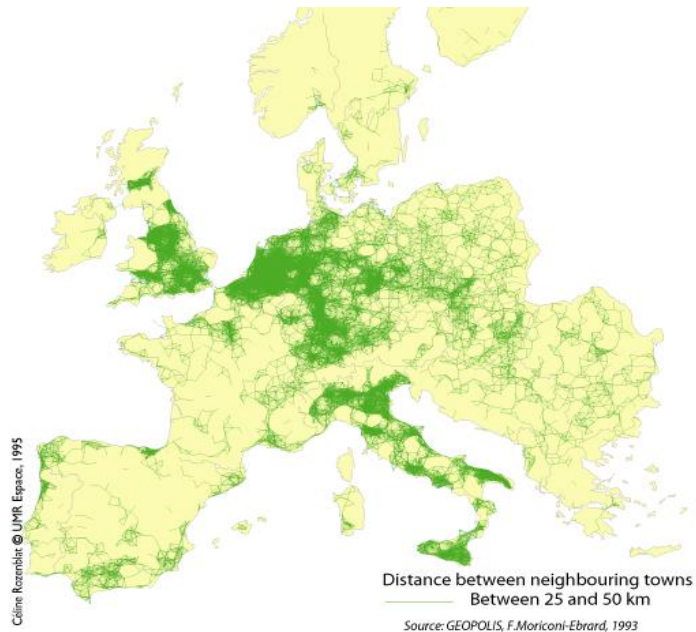
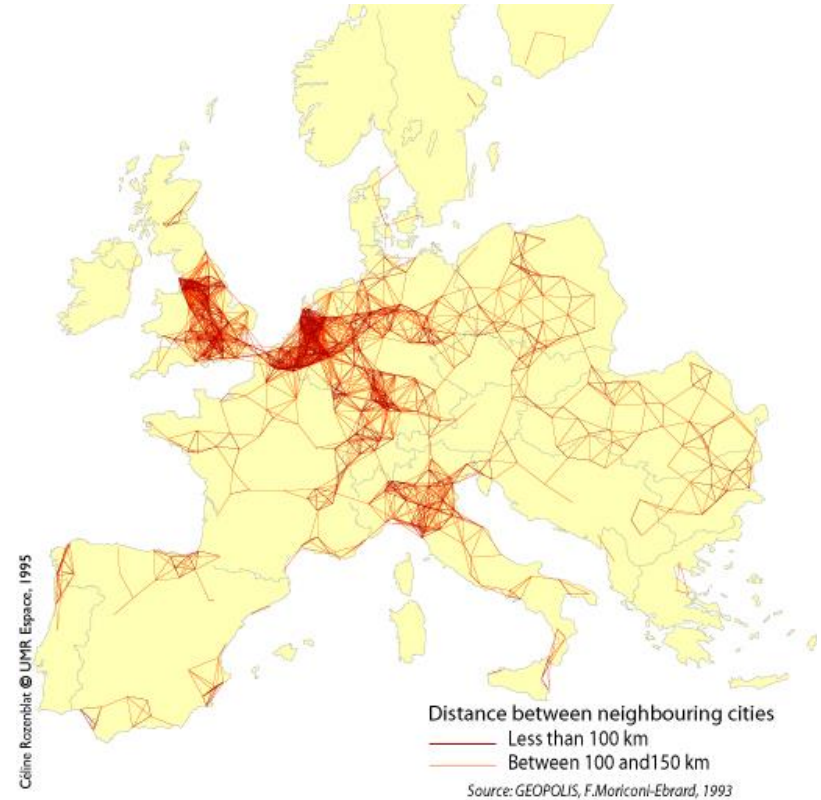
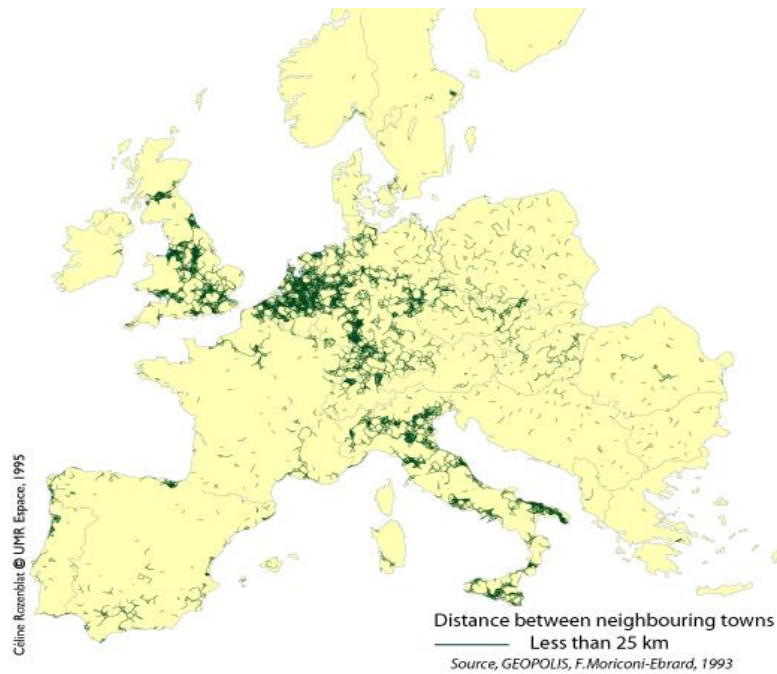


[GeoDiverCity, Pumain et al, Cybergegeo 2015]

# Applicable knowledge

- Statistical predictability of city growth and size for a few decades
- Largest metropolises are not « monstruopolises »
- Complexity → proactive adaptive strategies are necessary (imitation, or anticipation and risk), emulation (co-opetition)
- Robustness, variation and sustainability of urban systems (neither norm nor optimum)

# Robustness of three settlement styles in Europe



Céline Rozenblat, Mappemonde, 1995



# Socio-economic transformation: « discovery » of urban co-evolution with temporal multivariate analysis

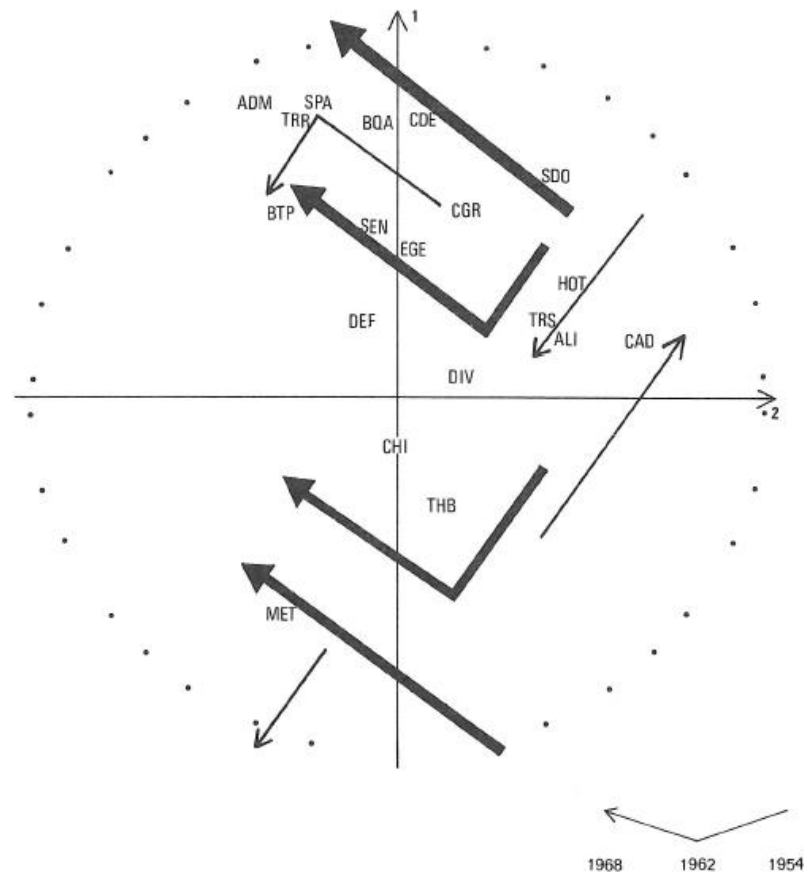
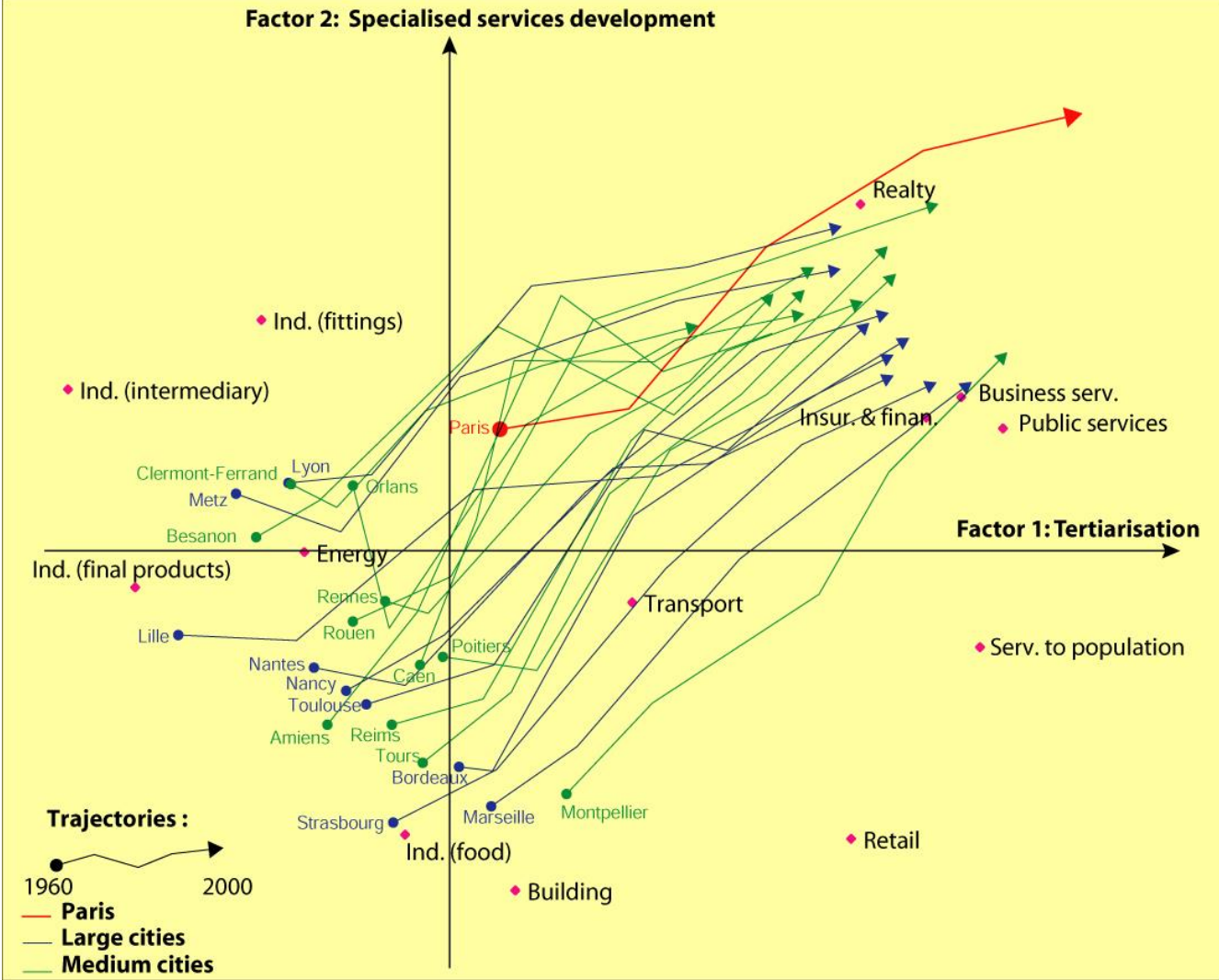


Figure 10 — Déplacements des villes dans la structure d'activité

[Pumain, Saint-Julien, 1978, Les dimensions du changement urbain]

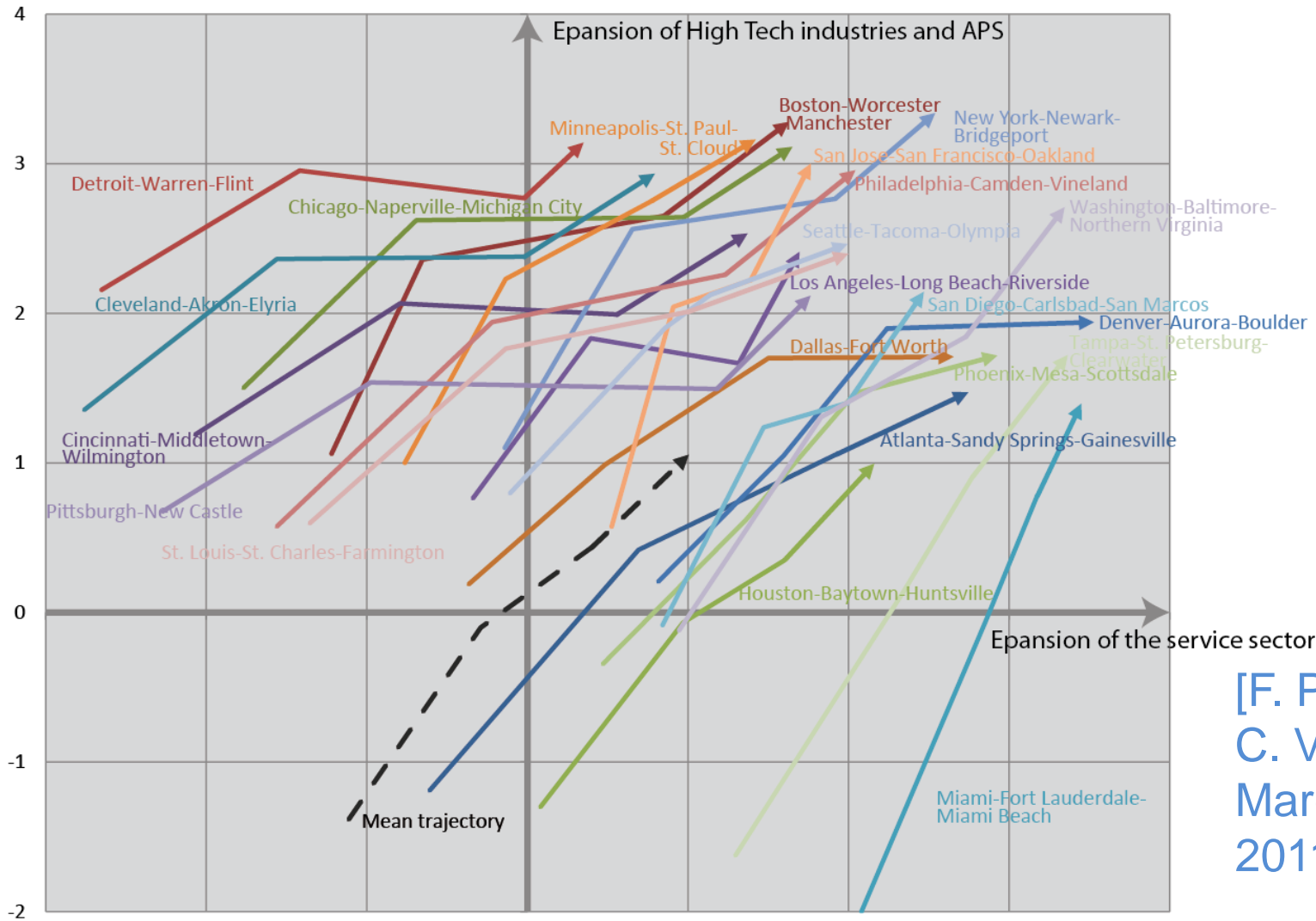
# Qualitative socio-economic co-evolution = propagation of societal innovation

PCA on  
French cities'  
economic  
profiles  
1960-2000



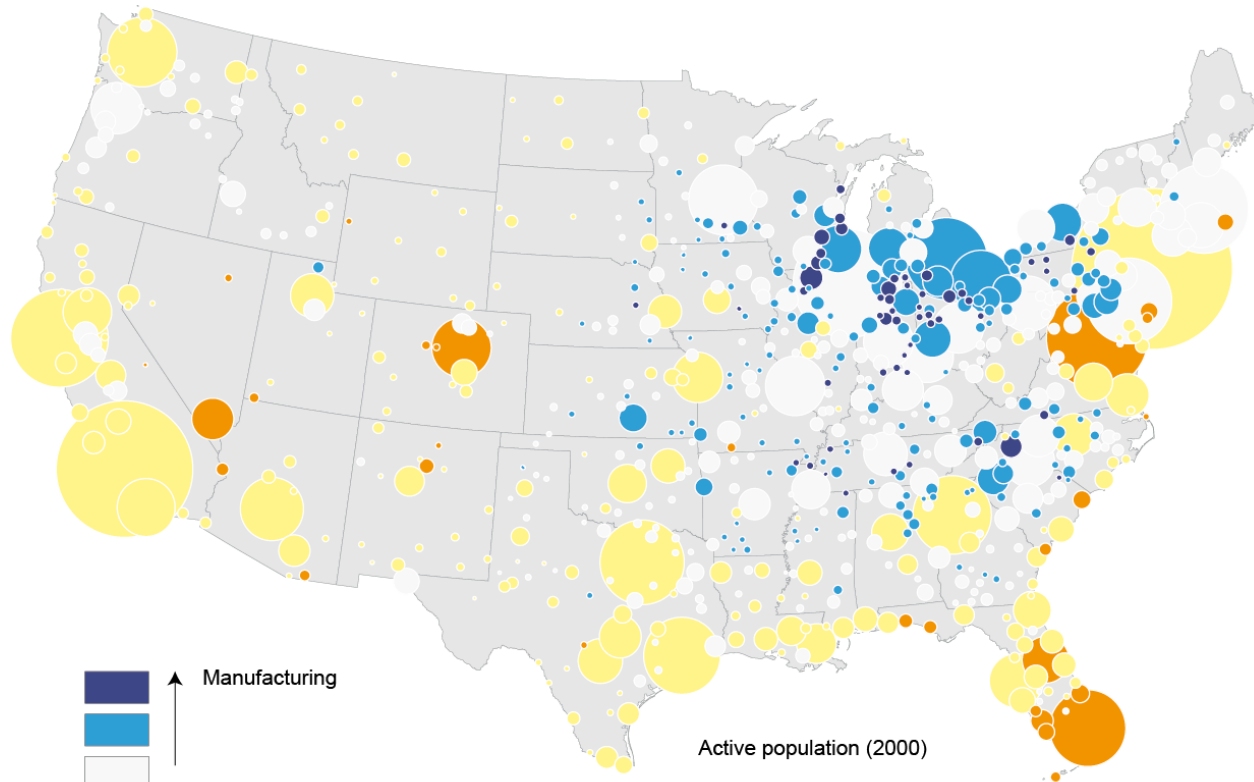
[F. Paulus, 2004]

# Co-evolution US cities >2 M inhab.



[F. Paulus  
C. Vacchiani-  
Marcuzzo,  
2011]

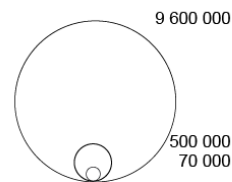
# Major economic differentiation of US cities =trace of innovation wave 19<sup>th</sup> century



1st factor of  
PCA=  
manufacturing/  
services  
(differentiation  
at regional  
scale)

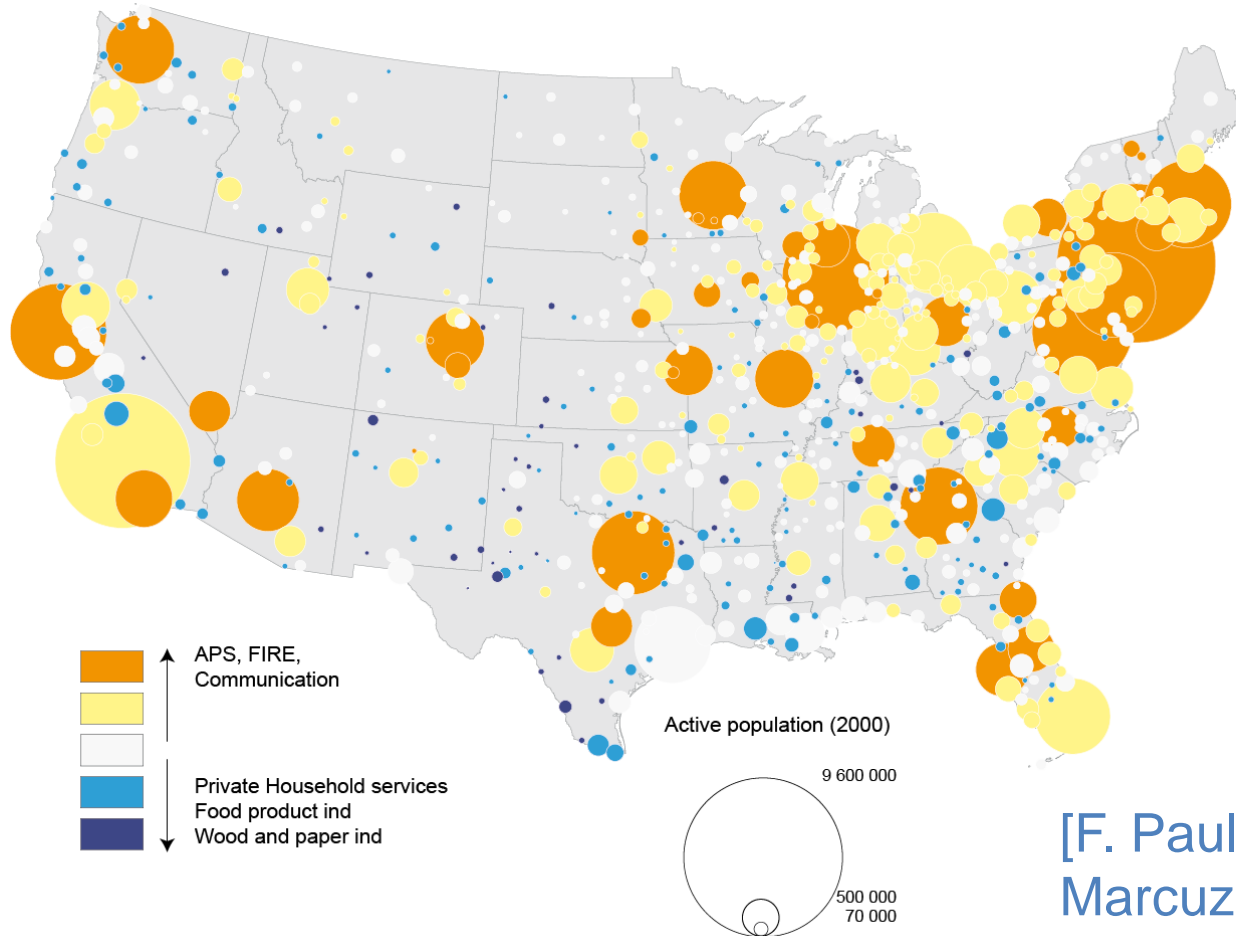


Active population (2000)



[F. Paulus, C. Vacchiani-Marcuzzo, 2011]

# Second economic differentiation = trace of recent economic cycles



**2d factor of  
PCA  
= new/old  
services  
(hierarchical  
diffusion)**

[F. Paulus, C. Vacchiani-Marcuzzo, 2011]

# Another progress in explanation

Size inequalities and qualitative socio-economic differences between cities are traces of their **co-evolution** (= interactive adaptation with feedbacks to the innovations they create)

Are now explained :

- systematic observed deviations / Gibrat's statistical model
- **emerging properties** of systems of cities (hierarchy and functional diversity)
- **bifurcations** of individual urban trajectories

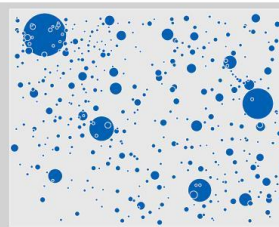
# Geographical ontology for urban systems

## Scale and urban systems

### Emerging structural properties

## Two levels: Cities and Systems of cities

#### Spatio-temporal scales



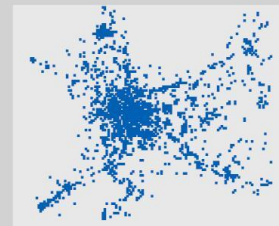
1 day

#### Emerging properties

Hierarchy  
Functional  
diversity  
Spatial pattern

#### Organization levels

**Macro: System  
of cities**  
(urban networks)

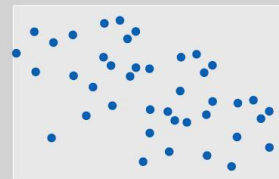


1 hour

Centrality  
Function  
Morphology  
"Ambiance urbaine"

**Meso: City**  
(urban areas)

#### Descriptors



Life cycle  
Profession  
Power

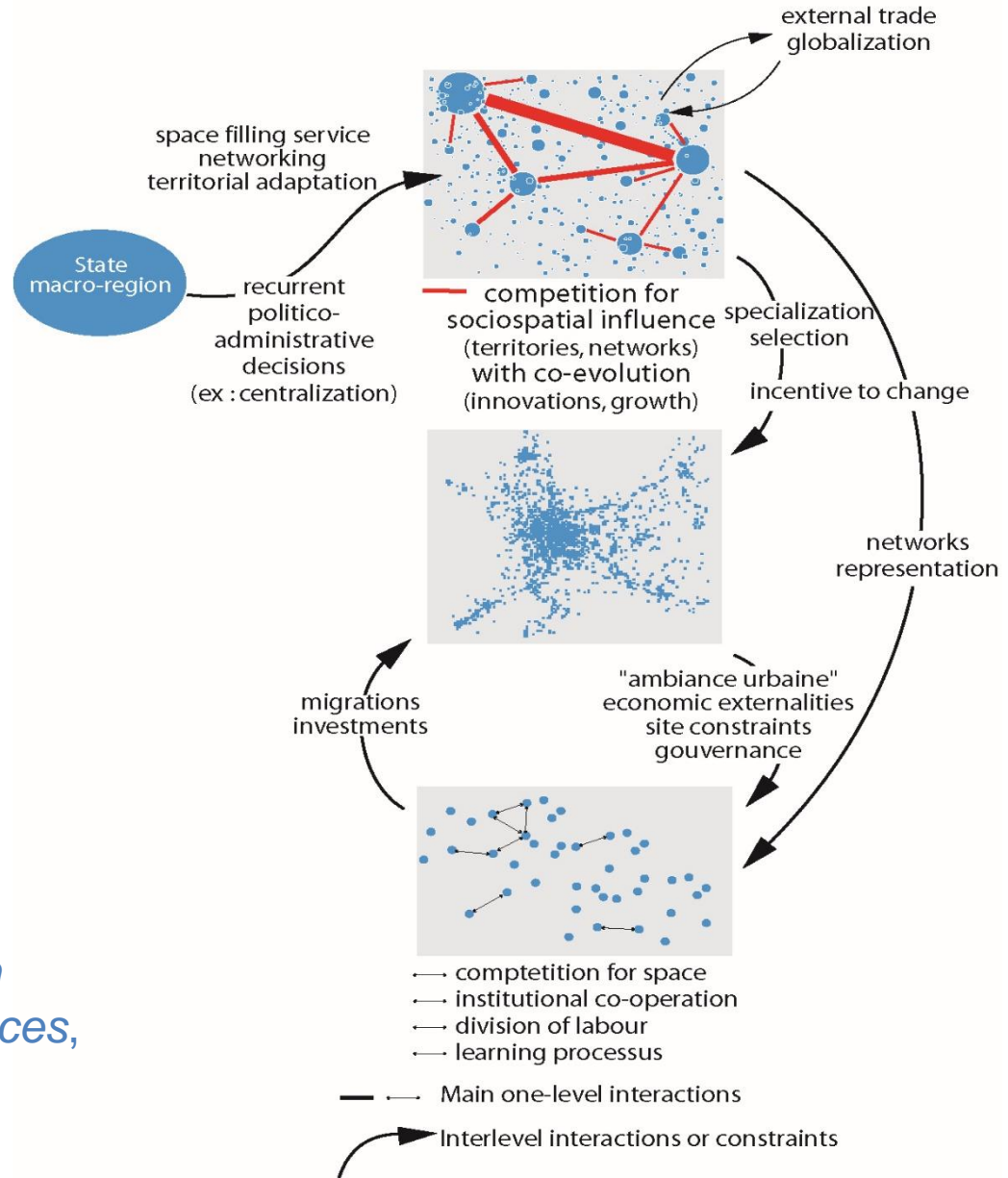
**Micro: Actors**  
(households, firms,  
institutions)

[Pumain D. *Hierarchy in natural and social sciences*, Springer, 2006]

# Constructive multi-levels interactions

## Scale and urban systems

### Constructive interactions



[Pumain D. *Hierarchy in natural and social sciences*, Springer, 2006]



# Urban trajectories/specialisation

$$X = P_{i_t} / P_{U_t}$$

( $P_{i_t}$  = population city i time t)

$P_{U_t}$  = urban system's total population time t)

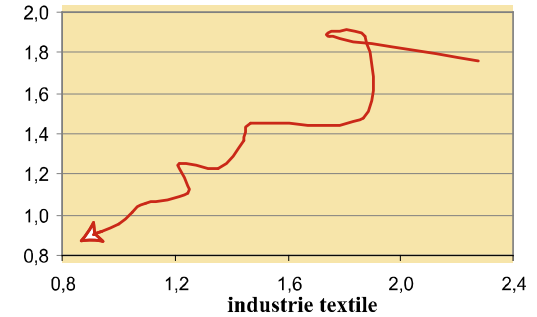
$$Y = P_{i_{t+1}} / P_{U_{t+1}}$$

[Bretagnolle, Vacchiani-Marcuzzo, Pumain, 2007]

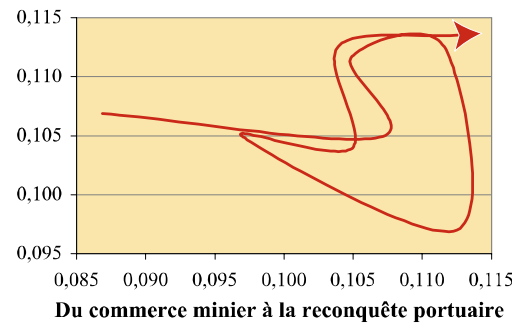
**Marseille**



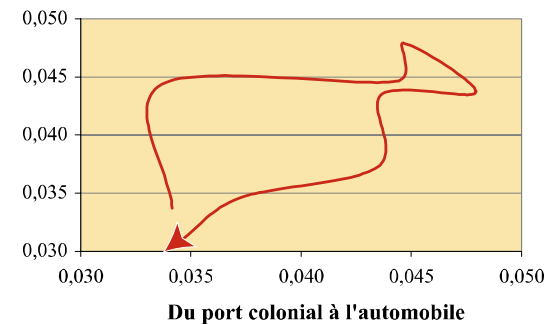
**Rouen**



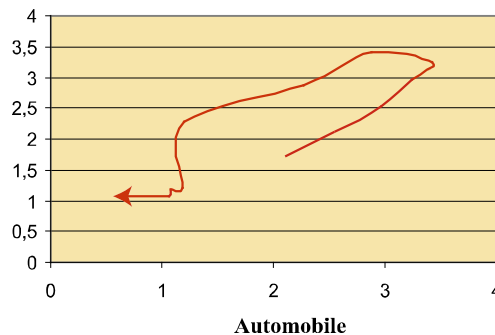
**Durban**



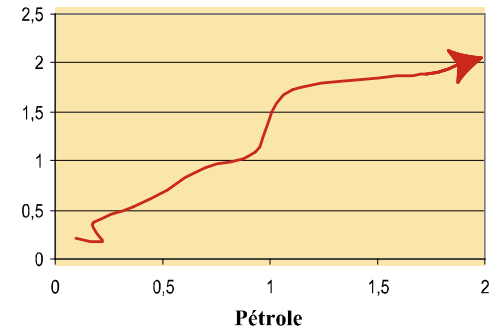
**Port-Elizabeth**



**Detroit**



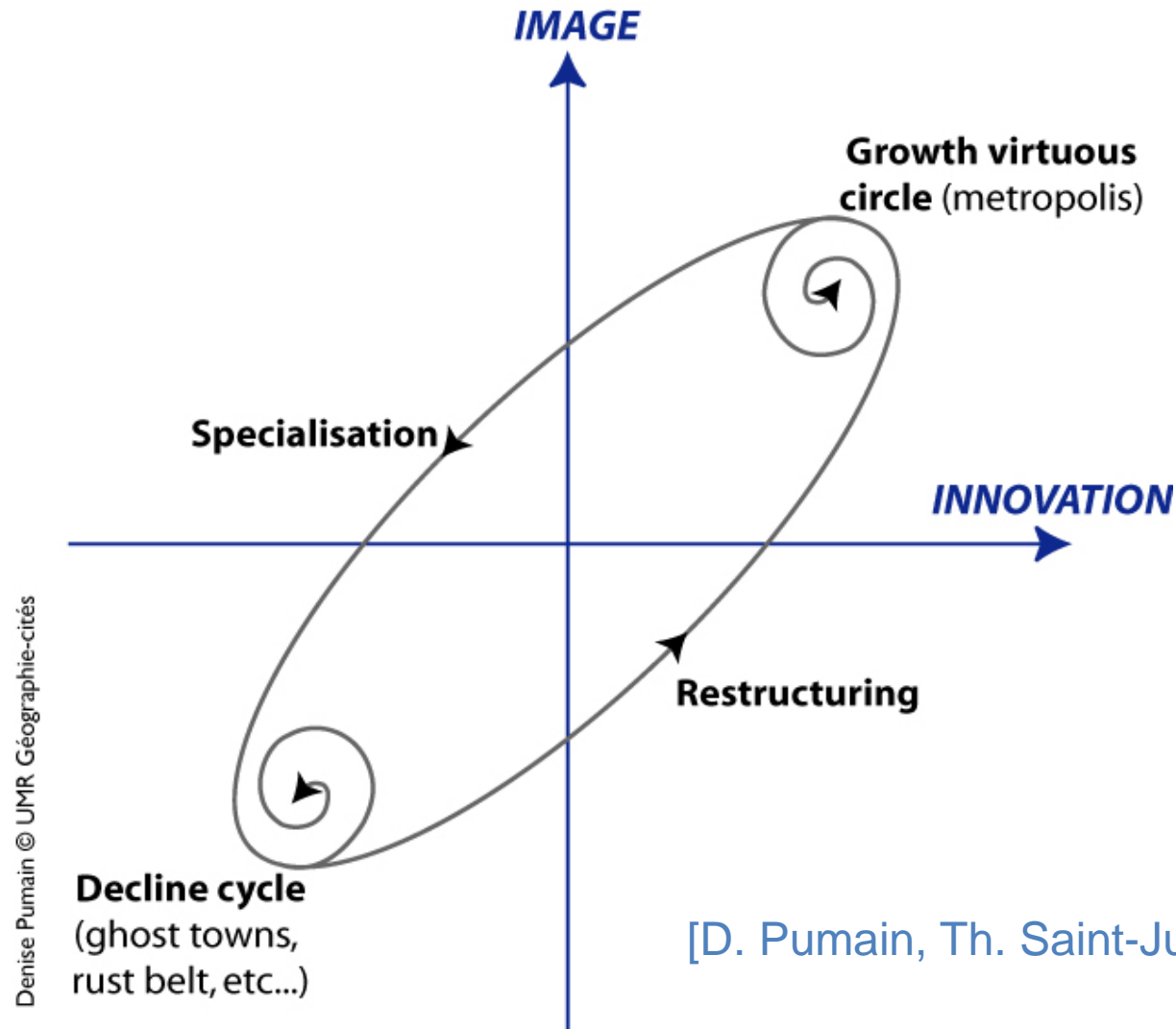
**Dallas**



en abscisses  $x = P_{i_t} / P_{U_t}$   
en ordonnées  $y = P_{i_{t+1}} / P_{U_{t+1}}$

$P_{i_t}$  : population de la ville au temps t  
 $P_{U_t}$  : population totale du système des villes au temps t

# Innovation as key factor of urban adaptive process



# Reconstructing urban trajectories with multi-agents systems

- **Reconstructing** past urban trajectories within their historical and geographical context is a first necessary step for testing the relevance of our theoretical explanation
- It is also a condition for ensuring the **quality of projections** estimating future relative positions of cities within inter-urban competition, thus for adjusting intelligent urban policies.

# SIMPOP: a multi-agents system

First application of MAS in geography !

Bura, Guérin-Pace, Mathian, Pumain, Sanders, Multi-agent systems and the dynamics of a settlement system.

*Geographical Analysis*, 1996, 2, 161-178

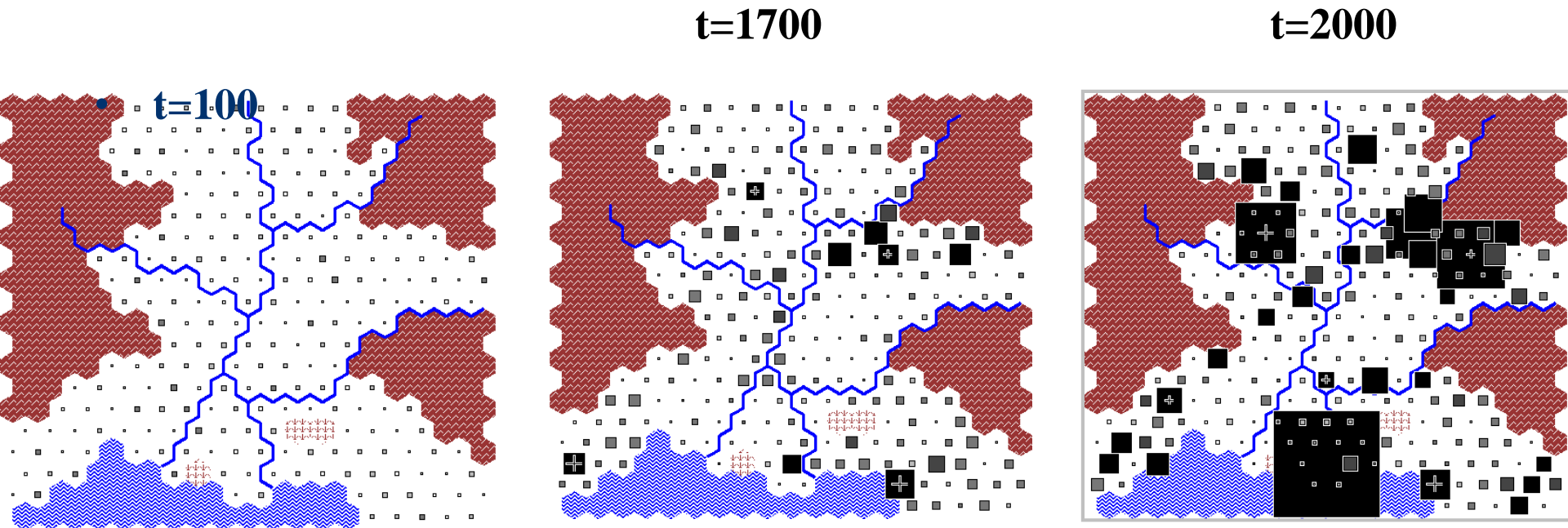
Main results:

- No emergence if no spatial interactions
- Emergence of a polycentric hierarchised system of cities even if homogeneous initial conditions
- A renewed innovation flow is necessary for maintaining structural properties of the system of cities

Pending questions: which validity of estimated parameters?

Conditions are sufficient , are they necessary?

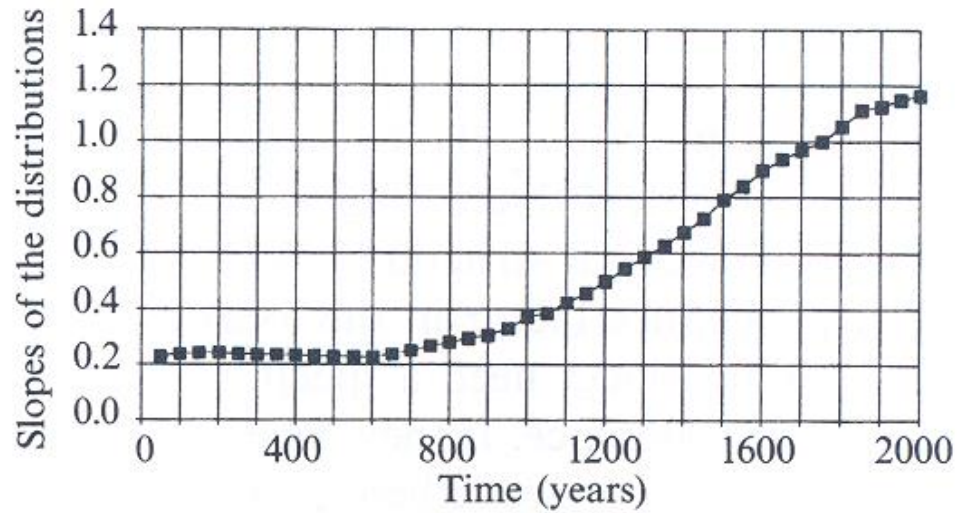
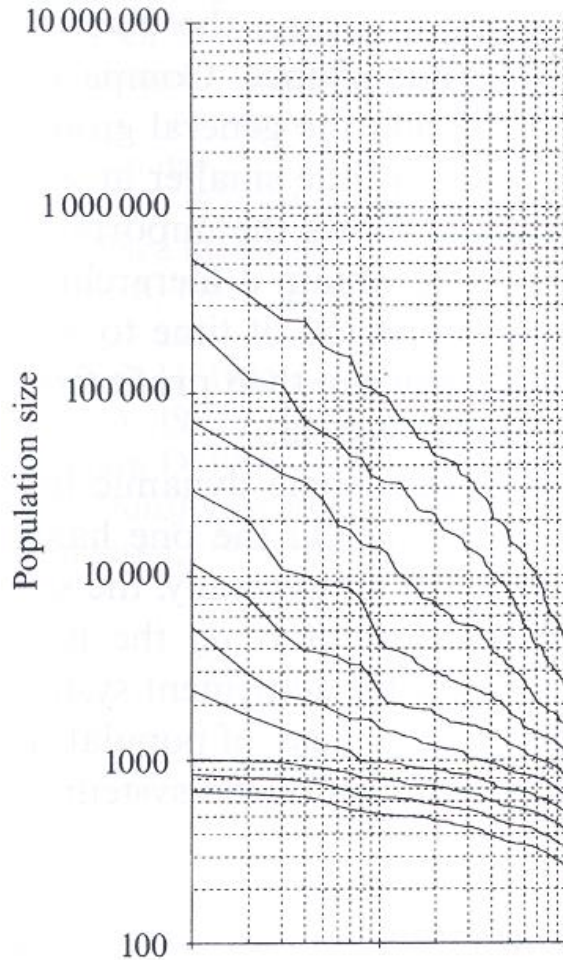
# The SIMPOP model: emergence of a polycentric system of cities



Starting from a rather regular distribution of settlements, a system of cities emerges, with a strong hierarchical and spatial organization

[Bura, Guérin-Pace, Mathian, Pumain, Sanders, 1996; Sanders et al.1997]

# Emerging hierarchical differentiation of the settlement system (rank-size distribution)



t = 2000

t = 1600

t = 0

*Source: SIMPOP model,  
Sanders et al. 1997*

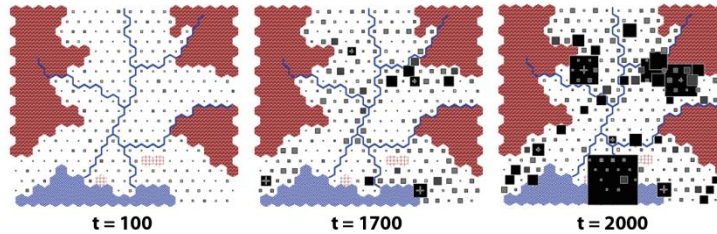
# Originality of SIMPOP Models

- Scale: national or continental integrated urban systems, long term
- Cities are agents : collective, immobile, heterogenous, evolving entities
- Main attributes: location, resources (labour force, capital), functions (10 types)
- Three levels: individual (firm or mayor, for scenarios), cities (local governance), national or multinational (global governance)
- Rules : stylised facts from comparative study of the observed evolution of integrated urban systems

# The Simpop family of simulation models

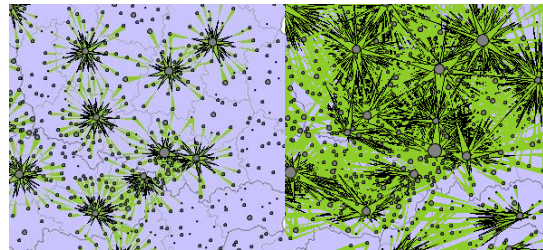
## URBAN EVOLUTIONARY THEORY

SIMPOP (1996)

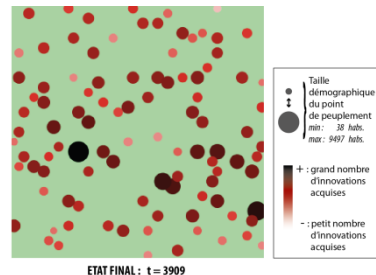


*First generation*

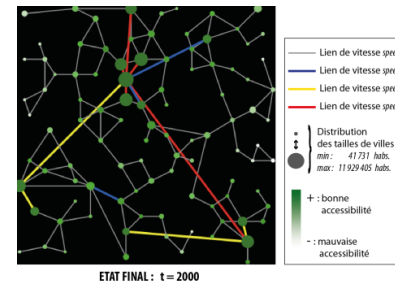
SIMPOP 2 (2006)



SimpopLocal  
(2012)



& SimpopNet  
(2012)



*Second generation*

MARIUS  
(2014)



# Two types of modelling teams

- 1995-2010 : 3 PhD students in computing from 3 different labs Ferber, Drogoul, Giavitto/Hutzler help geographers ( S. Bura, B. Glisse, T. Louail)  
→ Three models each in a different language (Smalltalk, Swarm, C++...), not reusable

**Institutional event** : ERC adv. grant GeoDiverCity

- 2010-2015: **real daily team work** between 4 computer scientists (Reuillon, Leclaire, Chapron, Cherel) and PhD in geography and geomatics (C. Schmitt, C. Cottineau, S. Rey-Coyrehourcq, E. Swerts, A. Ignazzi, S. Baffi, O. Finance)  
→ **Models** on systems of cities in Europe, USA, BRICS with **OpenMOLE platform** (evolutionary algorithms and distributed computing)

# Further advances in explanation

- No counter-urbanisation ( $\neq$  Berry, 1976), increasing hierarchisation / Gibrat' model prediction

(Bretagnolle, Pumain, Rozenblat, 1997, *Cybergeo*, 61, Bretagnolle, Mathian, Pumain, Rozenblat 2000, *Cybergeo* 131, Bretagnolle, Paulus, Pumain 2002, *Cybergeo*, 219)

➔ « metropolisation » and « simplification from below of urban hierarchies (cf. « shrinking cities »)

- « Global cities since Middle Ages » (Bretagnolle, Pumain, 2010, *Urban Studies*)

# Urban trajectories to reconstruct

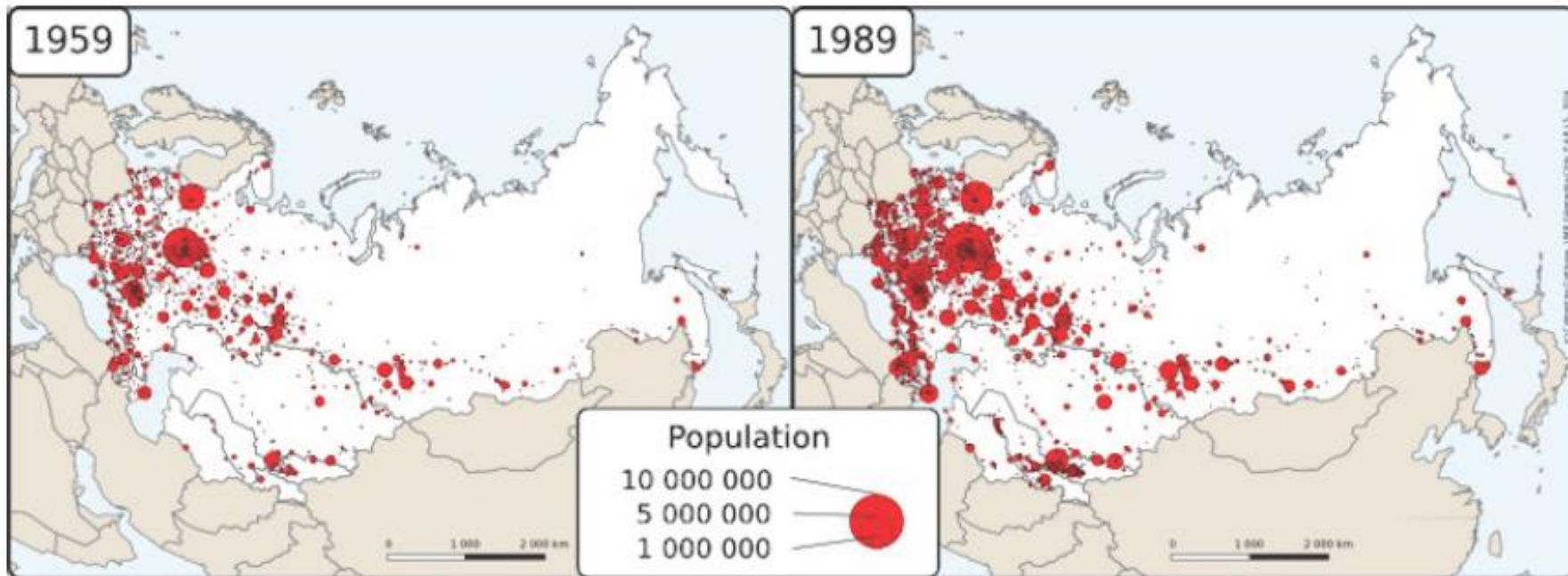


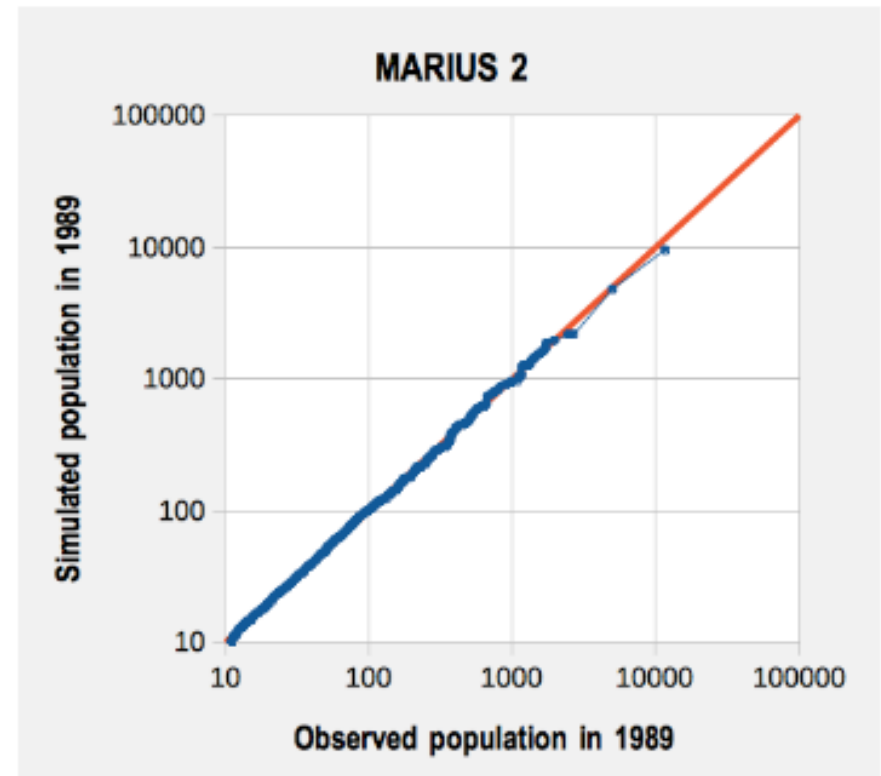
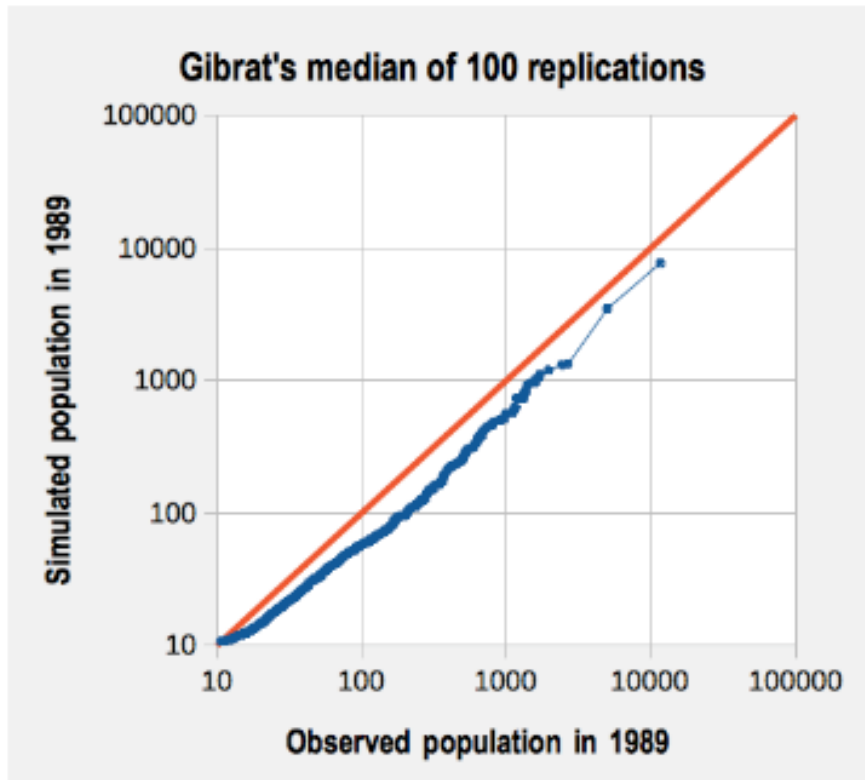
Figure 2. Empirical spatial and hierarchical distribution of cities in the post-Soviet space  
source: DARIUS, 2014

*Cottineau et al., 2015, JASS*

# Networking boosts urban growth: model with interaction fits better than random growth

**Gibrat's model**

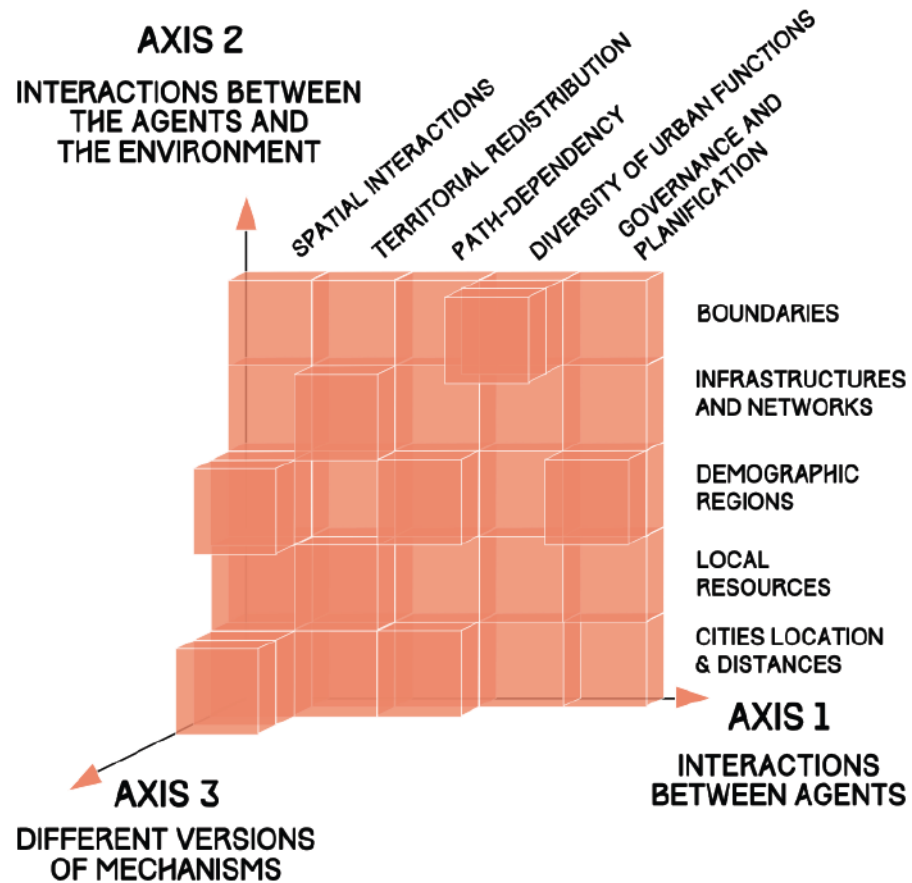
**model with interactions**



*Cottineau, 2014*

# New modelling method: building multi-models

## MARIUS



# Toward providing proofs in HSS

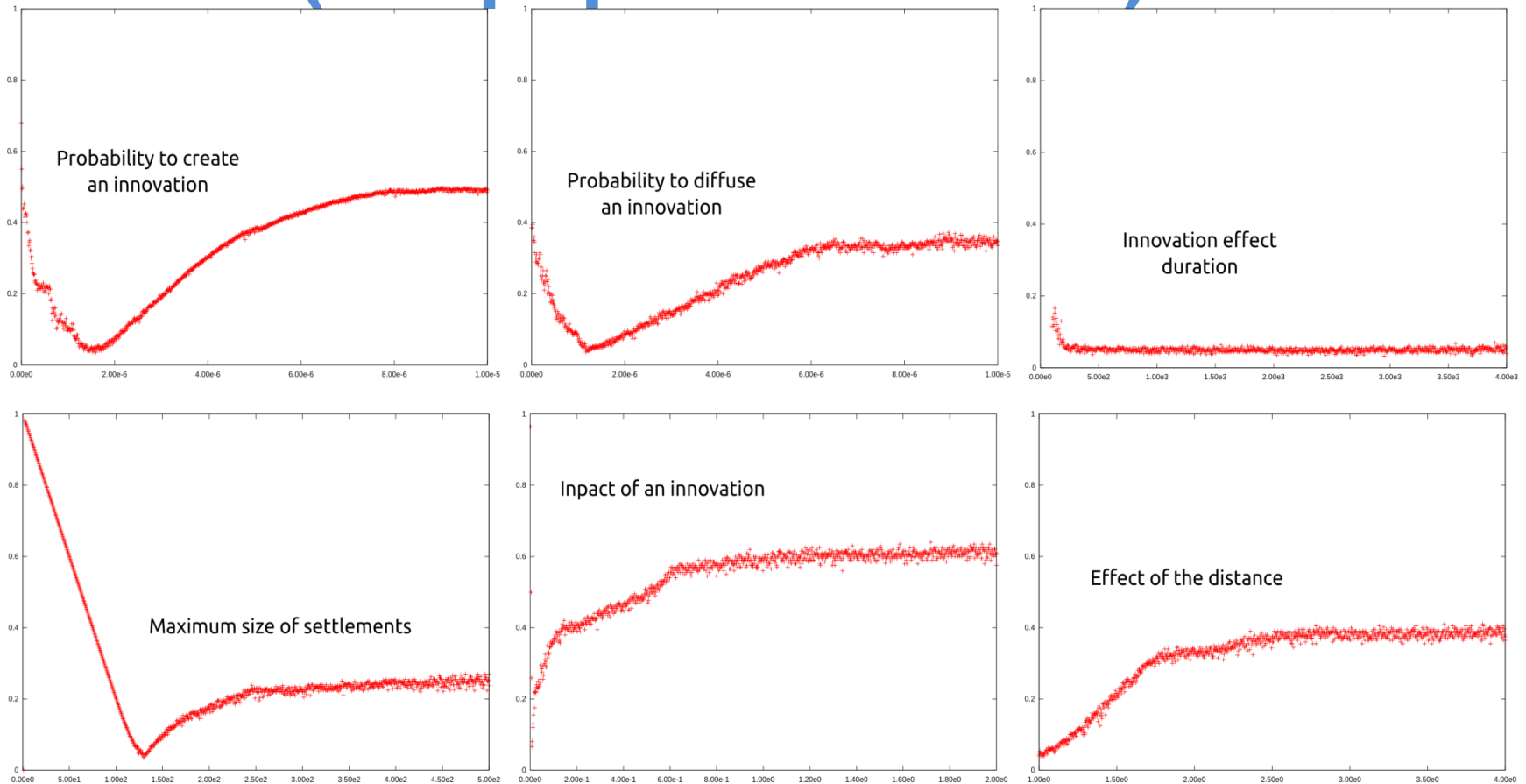
With SimpopLocal model (Clara Schmitt & Sébastien Rey-Coyrehourcq) and simulation platform OpenMole (Romain Reuillon, Mathieu Leclaire)

→ Proof: hypotheses are sufficient... **and necessary!**

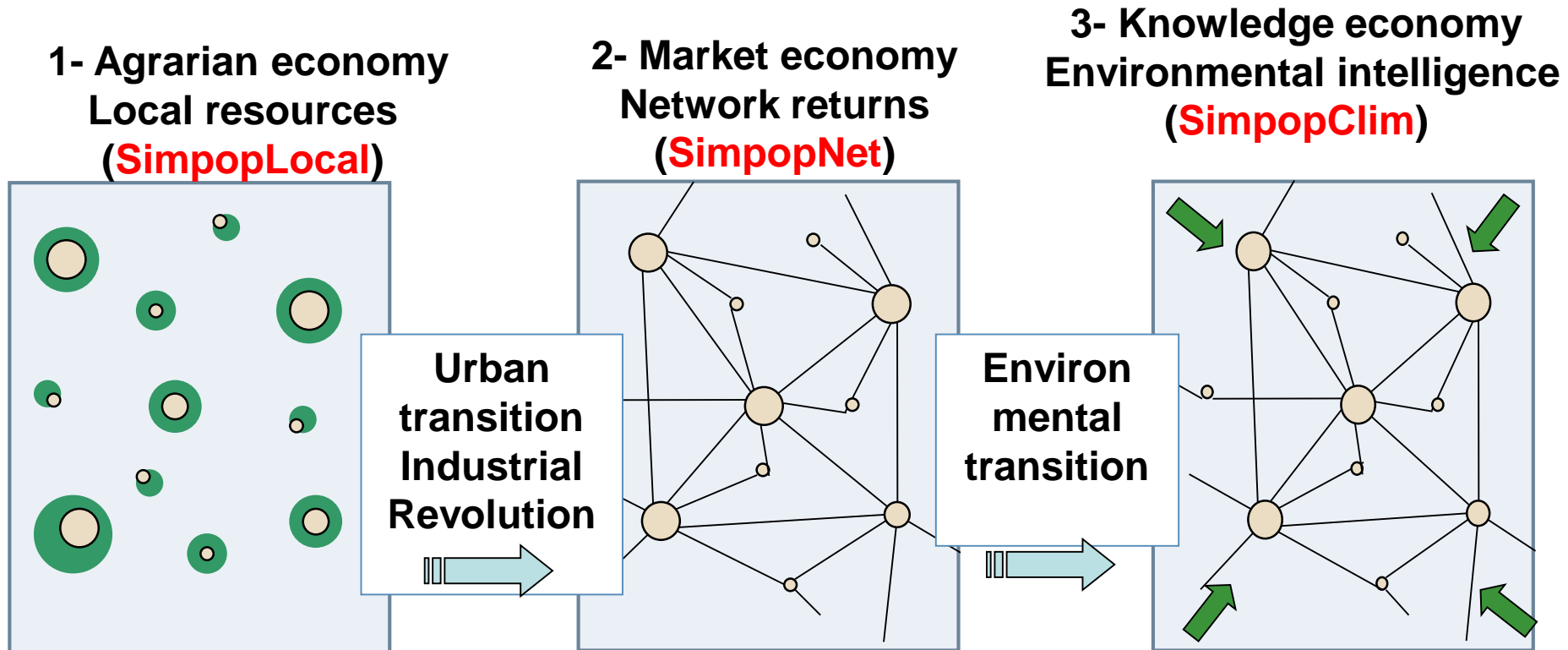
→ Schmitt C., Rey-Coyrehourcq S., Reuillon R., Pumain D., 2015, **Half a billion simulations, Evolutionary algorithms and distributed computing** for calibrating the SimpopLocal geographical model, *Environment and Planning B*, 42, 2, 300-315.

- **Calibration profile:** Romain Reuillon

# Best solutions in parameter space (SimpopLocal model)



# Three stages in the evolution of urban systems (consolidated evolutionary theory)



*SIMPOP models: France Guérin-Pace, Lena Sanders, Hélène Mathian with Stéphane Bura, Benoît Glisse, Thomas Louail (and Jacques Ferber, Alexis Drogoul, Jean-Louis Giavitto, Guillaume Hutzler). Anne Bretagnolle, Clara Schmitt, Sébastien Rey, Clémentine Cottineau, Elfie Swerts, Céline Vacchiani-Marcuzzo (with Romain Reuillon, Mathieu Leclaire, Paul Chapron, Guillaume Cherel )*



# Discussion

Thanks to OpenMole, a **step forward** assessing the level of generality of urban theories vs identifying regional variations:

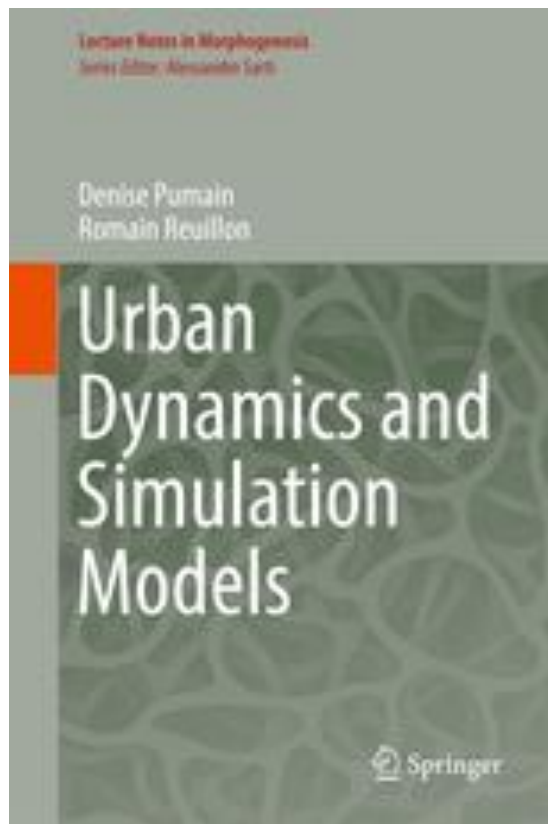
- Multimodelling (incremental modelling with **generic computing and distributed computing tool**) produces a population of optimal solutions and compares their contribution to model fit = the explanatory power of different mechanisms at reconstructing urban trajectories
- For non-compatible models: comparing respective performances of bi-objective Pareto fronts

## Open questions

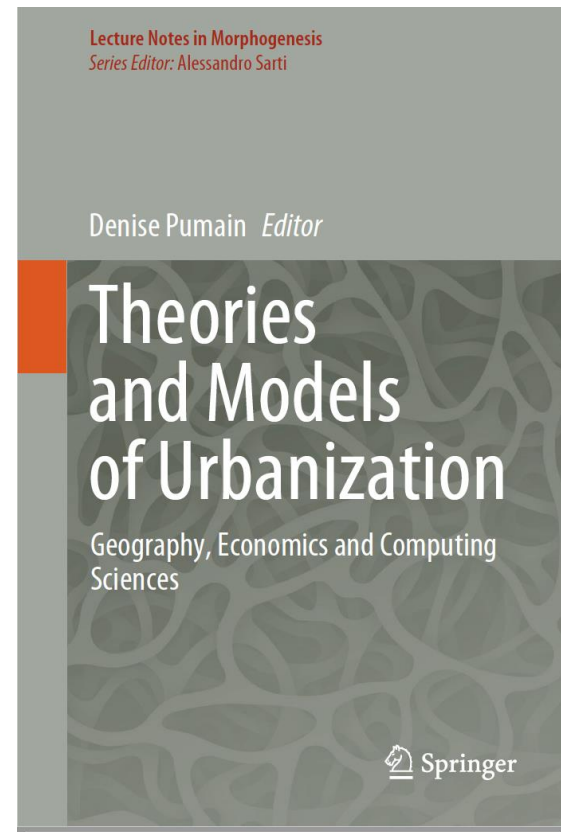
- How to compare the explanatory power of models with different structures?
- Observations or synthetic data for simulations?

# Thank you for your attention!

<http://geodiversity.parisgeo.cnrs.fr>



2017



2020